

UIL Calculator Applications

Test 09E
(TMSCA State)

DO NOT OPEN THE TEST UNTIL INSTRUCTED TO BEGIN

- I. Calculator Applications rules and scoring—See UIL Constitution
- II. How to write the answers
 - A. For all problems except stated problems as noted below—write three significant digits.
 - 1. Examples (* means correct but not recommended)
 - Correct: 12.3, 123, 123.*, $1.23 \times 10^*$, 1.23×10^0 *
 - 1.23×10^1 , 1.23×10^{01} , .0190, 0.0190, 1.90×10^{-2}
 - Incorrect: 12.30, 123.0, $1.23(10)^2$, $1.23 \cdot 10^2$, 1.230×10^2 , 1.23×10^2 , 0.19, 1.9×10^{-2} , 19.0×10^{-3} , 1.90×10^{-2}
 - 2. Plus or minus one digit error in the third significant digit is permitted.
 - B. For stated problems
 - 1. Except for integer, dollar sign, and significant digit problems, as detailed below, answers to stated problems should be written with three significant digits.
 - 2. Integer problems are indicated by (integer) in the answer blank. Integer problems answers must be exact, no plus or minus one digit, no decimal point or scientific notation.
 - 3. Dollar sign (\$) problems should be answered to the exact cent, but plus or minus one cent error is permitted. Answers must be in fixed notation. The decimal point and cents are required for exact-dollar answers.
 - 4. Significant digit problems are indicated by underlined numbers and by (SD) in the answer blank. See the UIL Constitution and Contest Manual for details.
 - III. Some symbols used on the test
 - A. Angle measure: rad means radians; deg means degrees.
 - B. Inverse trigonometric functions: arcsin for inverse sine, etc.
 - C. Special numbers: π for 3.14159 ...; e for 2.71828 ...
 - D. Logarithms: Log means common (base 10); Ln means natural (base e); exp(u) means e^u .



09E-1. $-9.43 + 6.6 - 21.1$ ----- 1= _____

09E-2. $(0.321 + 0.423) \times (-0.737) - 0.875$ ----- 2= _____

09E-3. $(\pi - 3.02 + 16.5) \times (-2.91) - 521$ ----- 3= _____

09E-4. $\frac{9940 + 32300 - 29900}{(-747)(503)(-111)}$ ----- 4= _____

09E-5. $\frac{(469 + 373 - 586)(71.9)}{(904)(249)(-976)}$ ----- 5= _____

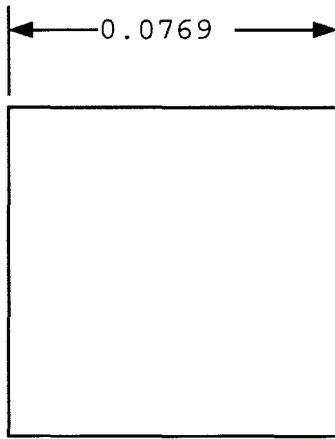
09E-6. What is the square of the product of 4.56 and 7.65? --- 6= _____

09E-7. What is the sum of the number of days in a week, the number of cards in a deck (no jokers) and the number of feet in the playing length of a football field? ----- 7= _____ integer

09E-8. Frank runs a mile in 7 min 25 sec. What is his time in a 26.22 mile marathon if his velocity decreases by 10%? ----- 8= _____ hr

09E-9.

SQUARE

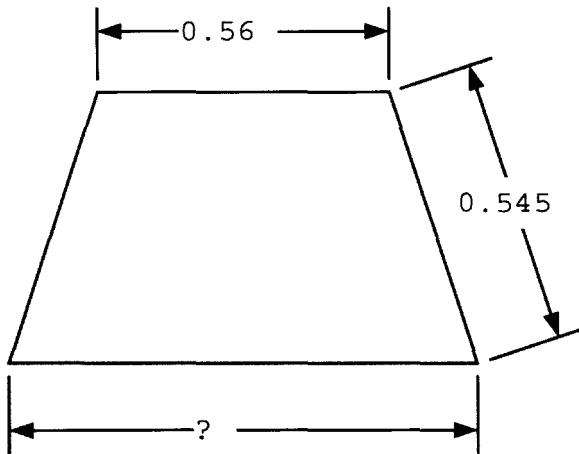


Area = ?

09E-9 = _____

09E-10.

ISOSCELES TRAPEZOID



Perimeter = 2.55

09E-10 = _____

09E-11. $\frac{(6.6 + 4.36)(5.76 + 17.3)}{(-8.39)(0.79)(8650 - 9860)}$ ----- 11= _____

09E-12. $\frac{(-114 + (5.67)(3.62)(-5.68))}{(0.292 + 0.414)(-5.77)(1.19 + 0.722)}$ ----- 12= _____

09E-13. $\frac{(-4.79 \times 10^{-5} - 5.28 \times 10^{-5})\{36300 + (-86.8)(-71.9)\}}{(-6.45)(-0.157 + 0.155)(94.3)(25.6)}$ ----- 13= _____

09E-14. $\frac{(1030 + 761 - 552)(0.00402 + 0.00854 - 0.00307)}{(-4.71 - 0.524)(-3.2)(3.51 - 0.943)}$ ----- 14= _____

09E-15. $\frac{(\pi + 1.47)}{8.69 - 23.1} + \frac{-0.575}{85.3 + 90.9} + \frac{(0.147)(639 - 312)}{(-173)(0.428)}$ ----- 15= _____

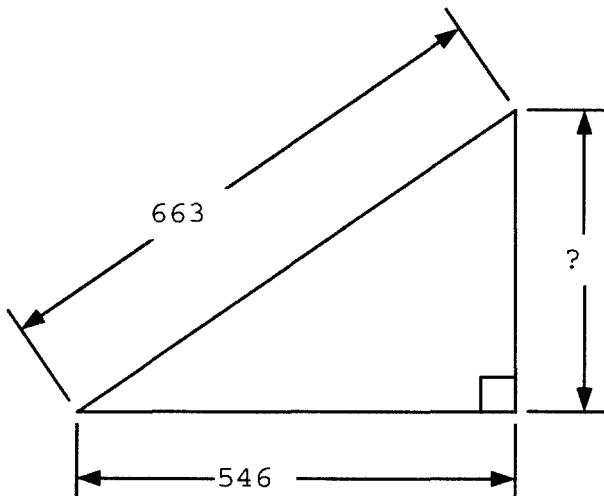
09E-16. A plane flies to a destination in 38 minutes but it takes a car 3.4 hr to get there. What is the percent difference in the average traveling speed of a car and a plane? ----- 16= _____ %

09E-17. If a light-second is 186,000 miles, how many nanometers are there in a light-second? ----- 17= _____ nm

09E-18. In May 2008, a wildfire burned 4,000 acres near Santa Clara, California. How many Super-Walmarts does this area equate to if a Super-Walmart is 100,000 square feet? ----- 18= _____

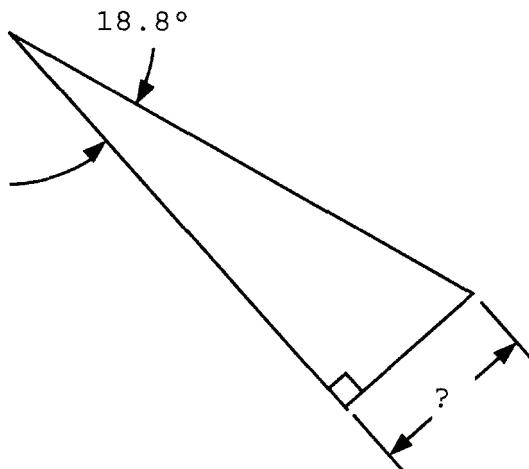
09E-19.

RIGHT TRIANGLE



09E-20.

RIGHT TRIANGLE



$$\text{Area} = 17.6$$

09E-19 = _____

09E-20 = _____

09E-21. $\frac{-0.212 + 1 / (-4.68)}{1 / (1.57) + 3.14} + \frac{1}{(-5.17)}$ ----- 21= _____

09E-22. $\frac{1}{8.98 + 9.44} + \frac{1}{2.74 - 6.87} + \frac{1}{(17.4)}$ ----- 22= _____

09E-23. $(0.23)(3.14)\sqrt{(-0.466)^2 / 0.282} + 1 / \sqrt{\pi} + 2.01$ ----- 23= _____

09E-24. $\left[\frac{\pi + 0.855 + \sqrt{0.867 / 0.911}}{-1.99 + 1.93} \right]^2$ ----- 24= _____

09E-25. $\frac{\sqrt{1.87 + 1.21 + (27.2) / (9.67)}}{9.79 + 4.91}$ ----- 25= _____

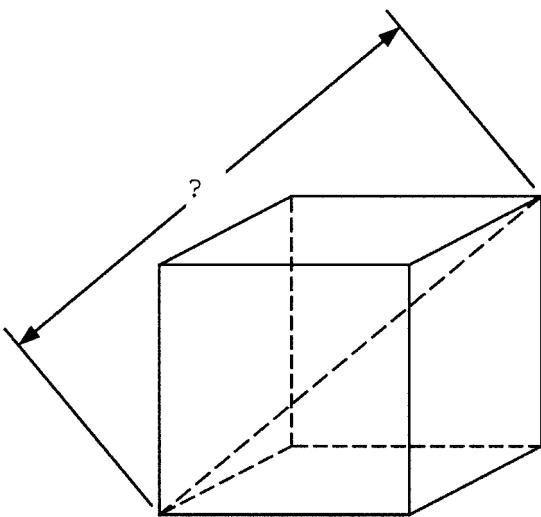
09E-26. Gene invests \$100 at 4% annual interest. How long will it take to double his money? ----- 26= _____ yr

09E-27. The monthly payment MP equals $P \left[i + \frac{i}{(1+i)^n - 1} \right]$ where P is the principal, i is the annual interest rate divided by 12 and n is the number of months. If Harry can afford to pay \$350 monthly for a car, and the annual interest rate is 5.4%, how many months will it take him to pay out a \$19,900 loan? -- 27= _____ mo(integer)

09E-28. NASA sent the Phoenix Probe to Mars in 2007/08. It traveled 423 million mi on the trip from Earth to Mars. If the mean orbital radii of the Earth and Mars are 1.496×10^8 km and 2.279×10^8 km, respectively, what is the percent difference in the average closest approach of the planet's and the distance Phoenix traveled? ----- 28= _____ % (SD)

09E-29.

CUBE

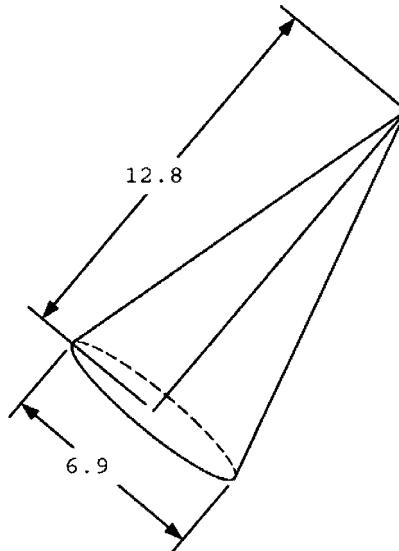


Total Surface Area = 0.912

09E-29 = _____

09E-30.

CONE



Volume = ?

09E-30 = _____

09E-31. $\left[\frac{-1.35 \times 10^7}{-9.05 \times 10^7 + 4.45 \times 10^7} + 0.454 \right] \times \{ 139 + (-11.8)^2 - \sqrt{20100} \} \quad -- \quad 31 = \underline{\hspace{2cm}}$

09E-32. $\sqrt{\frac{1 / (514 - 189)}{(798)(5.56 + 4.08)^2}} + (5.34)^2 (8.21 \times 10^{-6}) \quad ----- \quad 32 = \underline{\hspace{2cm}}$

09E-33. $\frac{(4.15 \times 10^5)^2 (3.19 \times 10^{-12} + 1.15 \times 10^{-12})}{33.2 + (-0.338)(-511)} + \frac{1}{\frac{1}{0.00341} + \frac{1}{(-0.00147)}} \quad 33 = \underline{\hspace{2cm}}$

09E-34. $\frac{[(812 - 87.7)(0.159 / 0.85)]^{1/2}}{(0.37)^2 + (0.123 + 0.278)^2 + 0.149} \quad ----- \quad 34 = \underline{\hspace{2cm}}$

09E-35. $\frac{\left[\frac{(862 + 330)}{(815 + 1030)} \right]^2 + \sqrt{\frac{0.0937 + 0.276}{\sqrt{0.156}}}}{((-149) / (-154))^2} \quad ----- \quad 35 = \underline{\hspace{2cm}}$

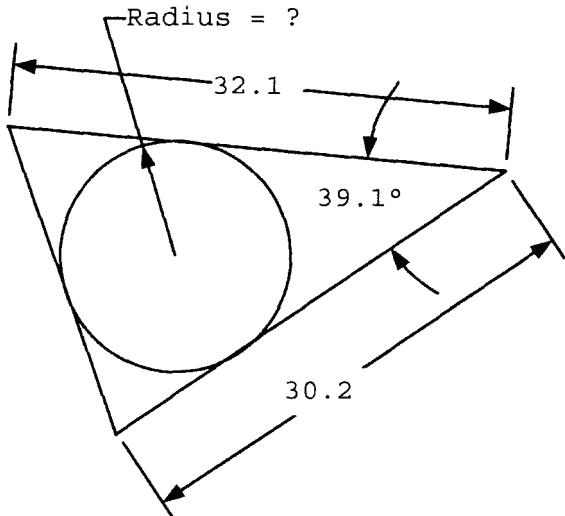
09E-36. The volume of water in the world's oceans is 317 million cubic miles which is 97.24% of the total water on the earth. What fraction of the earth's volume is water? ----- 36 = _____ %

09E-37. The Colossus of Rhodes, one of the seven wonders of the ancient world, stood 100 ft. It was clad with bronze plate averaging 0.5 in thickness. The surface area of a man 6 ft tall is 1.9 m^2 . Based on this, estimate the weight of bronze used in the Colossus. The density of bronze is 8.75 g/cm^3 . -- 37 = _____ lb

09E-38. Lenny starts with a full, 2-cup container of 30% salt solution. He divides the solution in half. To one half, he adds water to double the volume and refills the original container, discarding the left-over mixture. How many times must this procedure be done to dilute the original 30% solution down to just less than 5%? ----- 38 = _____ integer

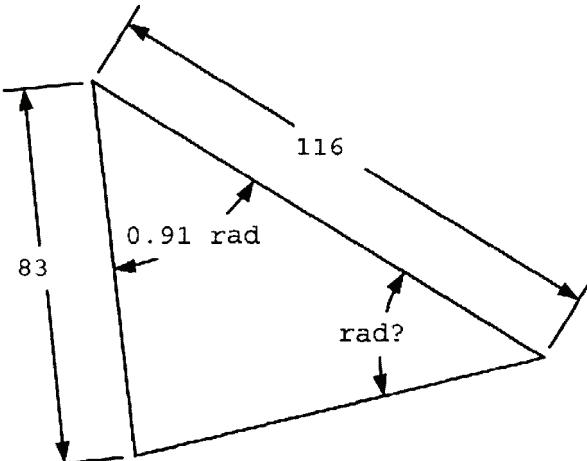
09E-39.

SCALENE TRIANGLE AND CIRCLE

09E-39 = _____

09E-40.

SCALENE TRIANGLE

09E-40 = _____

09E-41. $10^{-\{(0.109-0.698) / (0.183+0.0735)\}}$ ----- 41= _____

09E-42. $\frac{(-2.38 \times 10^{-6})}{(-1.65 \times 10^{-6})} \left[1 - e^{-(0.143)(0.418)} \right]$ ----- 42= _____

09E-43. $\frac{(-6.57 \times 10^7) \log(5.83 \times 10^7 - 3.73 \times 10^7)}{(1.41 \times 10^7)}$ ----- 43= _____

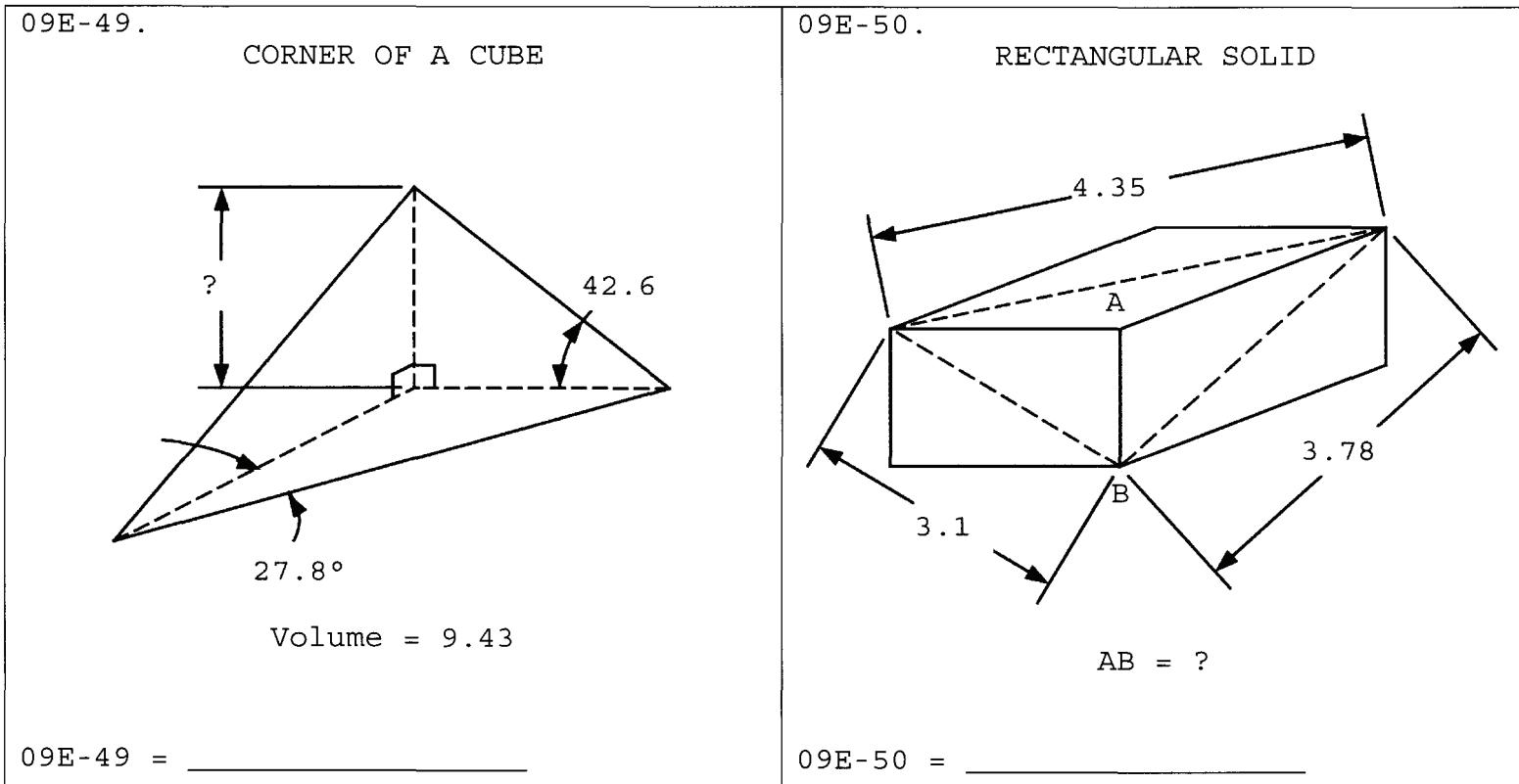
09E-44. $(1.15)^3 + (14.1 - 12.9)^2 \cdot 3$ ----- 44= _____

09E-45. (deg) $\sin \left[90^\circ \times \frac{(9.09 \times 10^5)}{(9.20 \times 10^5)} \right] + \cos \{167^\circ - 124^\circ\}$ ----- 45= _____

09E-46. A stone mason stacks rectangular cut stones to build a wall of fixed height and length. The stones are available in different sizes but have the same shape. The cost of a stone is proportional to its volume. If the wall materials cost is \$2000 when an 8-in stone is used, what is the cost of the wall when 10-in stones are used? ----- 46=\$ _____

09E-47. Jon is writing a book. He started keeping track of his daily writing after 78 pages were written. On consecutive days, he wrote 5 pages, 8 pages, 3 pages, 9 pages and 6 pages. Estimate the total time required for Jon to completely write the book if the finished book is 478 pages. ----- 47= _____ days

09E-48. (rad) What is the value of x between 0 and 2 if $\sin(x + 7) = x^3 \cos(5 - 2x)$? ----- 48= _____



09E-51. $\frac{10^{(0.64)} \times 10^{-(0.28)} + 0.311}{10^{(3.62+0.767)}} \quad 51 = \underline{\hspace{10cm}}$

09E-52. $\frac{(\pi - 2.97)e^{(0.841)(4.28)}}{e^{-(5.22-3.76)}} \quad 52 = \underline{\hspace{10cm}}$

09E-53. $(-65300) \ln \left[\frac{61800 + (14100)(3.33)}{76800 + 3.02 \times 10^5} \right] \quad 53 = \underline{\hspace{10cm}}$

09E-54. $\frac{(-15900 + 28900)^{-0.23}}{(87200)^{-(0.924+0.686)}} \quad 54 = \underline{\hspace{10cm}}$

09E-55. (rad) $\frac{\arctan\{5.62 + (2.59)(0.394)\}}{\arcsin\{(0.661 + 0.307)/2.09\}} \quad 55 = \underline{\hspace{10cm}}$

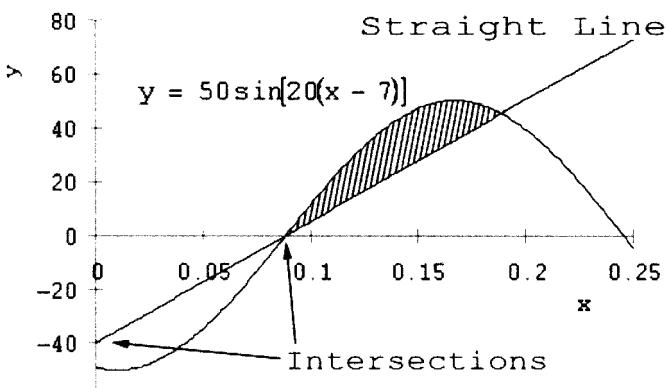
09E-56. What is the minimum value of x for the ellipse
 $3x^2 - 5x + y^2 = 238?$ $56 = \underline{\hspace{10cm}}$

09E-57. A backpacker is 2 miles away from a straight road and 10 miles away from a town. The road goes directly to the town. If the backpacker hikes at 3 mph off-road and 4 mph on the road, at what angle should she hike toward the road (directly towards the road is zero degrees) to get to the town as quickly as possible? $57 = \underline{\hspace{10cm}} \text{ deg}$

09E-58. Calculate p given that $B_3 = 263$, $C = \begin{bmatrix} 25 & 16 & 18 \\ 4 & 3 & 3 \\ 6 & 27 & 20 \end{bmatrix}$ and $D = \begin{bmatrix} 8 \\ 5 \\ p \end{bmatrix}$.
and $B = CD$. $58 = \underline{\hspace{10cm}}$

09E-59.

RADIAN

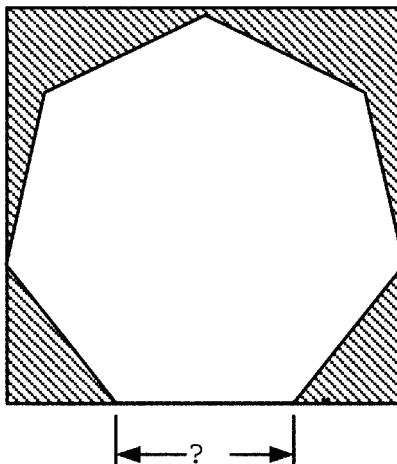


Hatched Area = ?

09E-59 =

09E-60.

REGULAR HEPTAGON AND SQUARE



Hatched Area = 867

09E-60 =

09E-61. $2 \log \sqrt{\frac{(6.72)(1.66)(4.22)}{(2.76)^3(9.53)^3}}$ ----- 61= _____

09E-62. (rad) $\frac{\sin(8.75)}{\cos(8.75)} \sqrt{1 - \{\sin(0.966 \times 5.27)\}^2}$ ----- 62= _____

09E-63. (rad) $\frac{1}{(6620)(0.111)} \ln\{(8.2) + (-6.81) \sin(1.44)\}$ ----- 63= _____

09E-64. $1 + (0.78) + \frac{(0.78)^2}{2} + \frac{(0.78)^3}{6} + \frac{(0.78)^4}{24}$ ----- 64= _____

09E-65. $\frac{1}{\sqrt{(36.3)^2 - (474)}} \ln \left\{ \frac{(36.6) - \sqrt{(36.3)^2 - (474)}}{(36.6) + \sqrt{(36.3)^2 - (474)}} \right\}$ ----- 65= _____

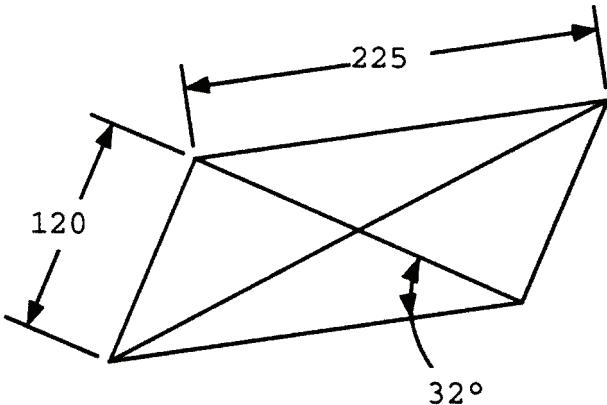
09E-66. Compass bearing is the angle in degrees measured clockwise from north. If Hank hikes 1.8 mi at a bearing of 250° and then hikes another 4 mi at 300° , how far is he from where he started? ----- 66= _____ mi

09E-67. What is the distance from the point $(18, 9)$ to the intersection of the lines $y = 8x+4$ and $y = -3x+6$? ----- 67= _____

09E-68. A thin-walled circular cylinder is filled 72% with water, closed up and then tipped over on a tabletop so it would roll if pushed. What is the height of the water level over the tabletop divided by the cylinder diameter? ---- 68= _____

09E-69.

PARALLELOGRAM



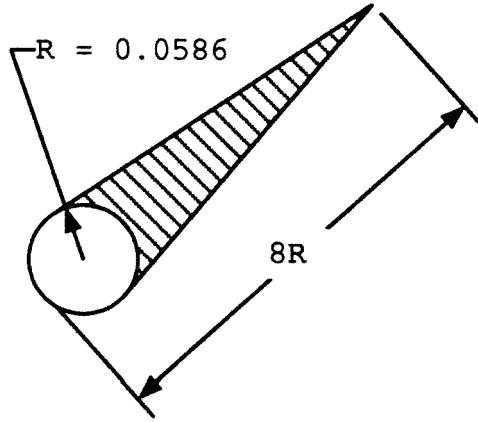
Product of Diagonals = ?

09E-69 = _____

09E-70.

CIRCLE, TANGENT LINES

Hatched Area = ?



09E-70 = _____

09E-1	= -23.9 = -2.39×10^1	09E-11	= 0.0315 = 3.15×10^{-2}	09E-21	= -0.306 = -3.06×10^{-1}
09E-2	= -1.42 = -1.42×10^0	09E-12	= 29.6 = 2.96×10^1	09E-22	= -0.130 = -1.30×10^{-1}
09E-3	= -569 = -5.69×10^2	09E-13	= -0.138 = -1.38×10^{-1}	09E-23	= 1.07 = 1.07×10^0
09E-4	= 0.000296 = 2.96×10^{-4}	09E-14	= 0.273 = 2.73×10^{-1}	09E-24	= 6870 = 6.87×10^3
09E-5	= -8.38×10^{-5}	09E-15	= -0.972 = -9.72×10^{-1}	09E-25	= 0.165 = 1.65×10^{-1}
09E-6	= 1220 = 1.22×10^3	09E-16	= 437 = 4.37×10^2	09E-26	= 17.7 = 1.77×10^1
09E-7	= 359 integer	09E-17	= 2.99×10^{17}	09E-27	= 66 integer
09E-8	= 3.60 = 3.60×10^0	09E-18	= 1740 = 1.74×10^3	09E-28	= 769 (3SD) = 7.69×10^2
09E-9	= 0.00591 = 5.91×10^{-3}	09E-19	= 376 = 3.76×10^2	09E-29	= 0.675 = 6.75×10^{-1}
09E-10	= 0.900 = 9.00×10^{-1}	09E-20	= 3.46 = 3.46×10^0	09E-30	= 160 = 1.60×10^2

09E-31	= 102	09E-41	= 198	09E-51	= 0.000107	09E-61	= -2.59
	= 1.02x10 ²		= 1.98x10 ²		= 1.07x10 ⁻⁴		= -2.59x10 ⁰
09E-32	= 0.000438	09E-42	= 0.0837	09E-52	= 27.0	09E-62	= -0.296
	= 4.38x10 ⁻⁴		= 8.37x10 ⁻²		= 2.70x10 ¹		= -2.96x10 ⁻¹
09E-33	= 0.00105	09E-43	= -34.1	09E-53	= 81500	09E-63	= 0.000504
	= 1.05x10 ⁻³		= -3.41x10 ¹		= 8.15x10 ⁴		= 5.04x10 ⁻⁴
09E-34	= 26.1	09E-44	= 3.04	09E-54	= 1.02x10 ⁷	09E-64	= 2.18
	= 2.61x10 ¹		= 3.04x10 ⁰				= 2.18x10 ⁰
09E-35	= 1.48	09E-45	= 1.73	09E-55	= 2.95	09E-65	= -0.0744
	= 1.48x10 ⁰		= 1.73x10 ⁰		= 2.95x10 ⁰		= -7.44x10 ⁻²
09E-36	= 0.125	09E-46	= \$2500.00	09E-56	= -8.11	09E-66	= 5.34
	= 1.25x10 ⁻¹				= -8.11x10 ⁰		= 5.34x10 ⁰
09E-37	= 129,000	09E-47	= 76.7	09E-57	= 48.6	09E-67	= 18.2
	= 1.29x10 ⁵		= 7.67x10 ¹		= 4.86x10 ¹		= 1.82x10 ¹
09E-38	= 7 integer	09E-48	= 1.77	09E-58	= 4.00	09E-68	= 0.677
			= 1.77x10 ⁰		= 4.00x10 ⁰		= 6.77x10 ⁻¹
09E-39	= 7.35	09E-49	= 2.93	09E-59	= 1.28	09E-69	= 60700
	= 7.35x10 ⁰		= 2.93x10 ⁰		= 1.28x10 ⁰		= 6.07x10 ⁴
09E-40	= 0.789	09E-50	= 1.58	09E-60	= 24.8	09E-70	= 0.0189
	= 7.89x10 ⁻¹		= 1.58x10 ⁰		= 2.48x10 ¹		= 1.89x10 ⁻²